



# CRITICALITY and NETWORK STRUCTURE drive emergent oscillations in a stochastic WHOLE-BRAIN MODEL

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J. Phys. Complex. 3 025010 (2022) ✉ GIORGIO.NICOLETTI.1@PHD.UNIPD.IT

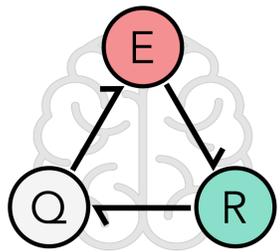
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Dynamical systems at their **CRITICAL POINT** are able to generate complex emergent patterns out of simple microscopical rules. In turn, their temporal evolution is also shaped and constrained by the underlying **NETWORK STRUCTURE**.

- What can we say about these combined effects in **WHOLE-BRAIN MODELS**?
- What is their role in driving **EMERGENT COLLECTIVE BEHAVIORS**?

## ► A STOCHASTIC WHOLE-BRAIN MODEL

● We study a three-state model - QUIESCENT, **EXCITED** or REFRACTORY - used by Haimovici et al. (PRL, 2013) to match resting state networks when tuned to a percolation-like critical point. However, not much was known about its dynamics!



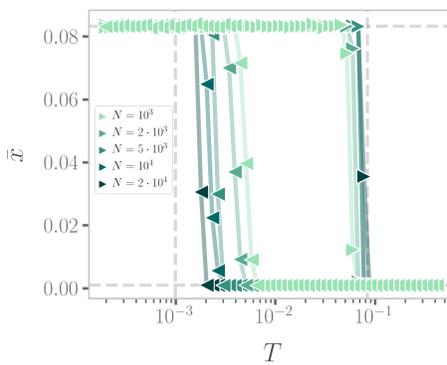
$$Q \rightarrow E \text{ if } \sum_j W_{ij} n_j^{(E)} > T \text{ or with prob. } r_1$$

$$E \rightarrow R \text{ with prob. } 1$$

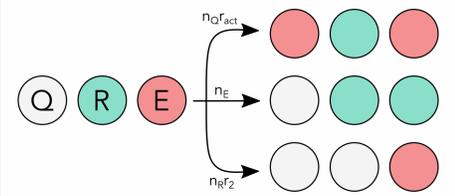
$$R \rightarrow Q \text{ with prob. } r_2$$

● We derive the exact **MEAN-FIELD APPROXIMATION** from the microscopic dynamics and study its behavior as we change the control parameter  $T$ , the input threshold for exciting a node.

We find no critical transition, but a **BISTABLE REGION** with hysteresis cycles between a high-activity and a low-activity fixed points.



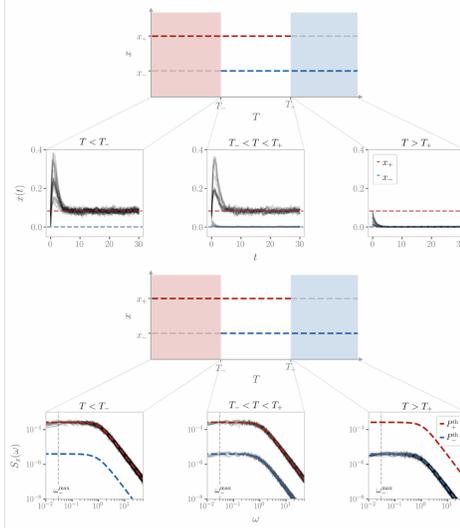
### MEAN-FIELD APPROXIMATION



$$x = \frac{n_E}{N} \quad y = \frac{n_R}{N} \quad \begin{pmatrix} \dot{x} \\ \dot{y} \end{pmatrix} = \begin{pmatrix} A_1(x, y) \\ A_2(x, y) \end{pmatrix}$$

$$A_1(x, y) = (1 - x - y)[r_1 + (1 - r_1)\Theta(x - T)] - x$$

$$A_2(x, y) = x - r_2 y$$

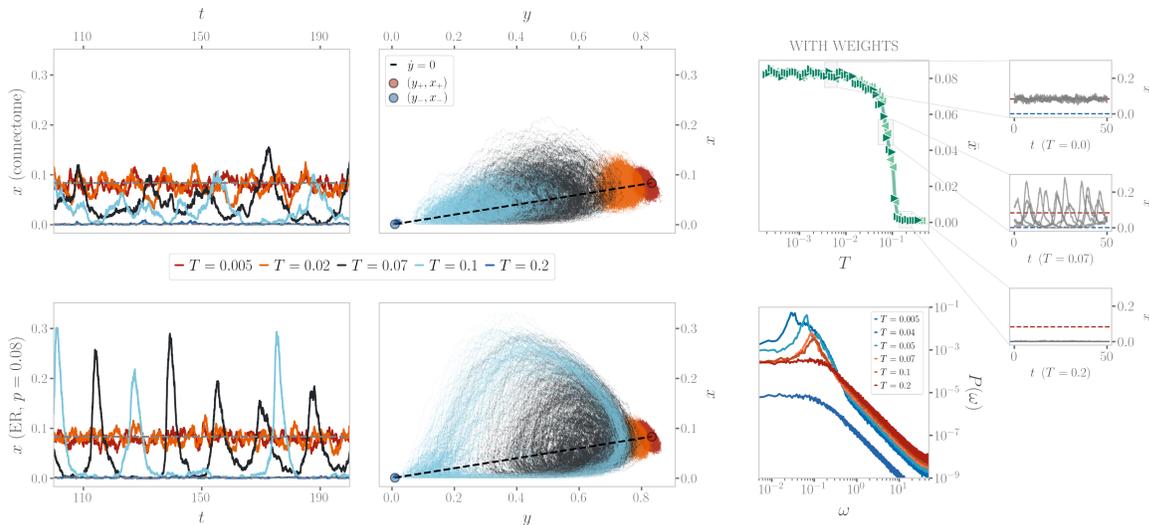
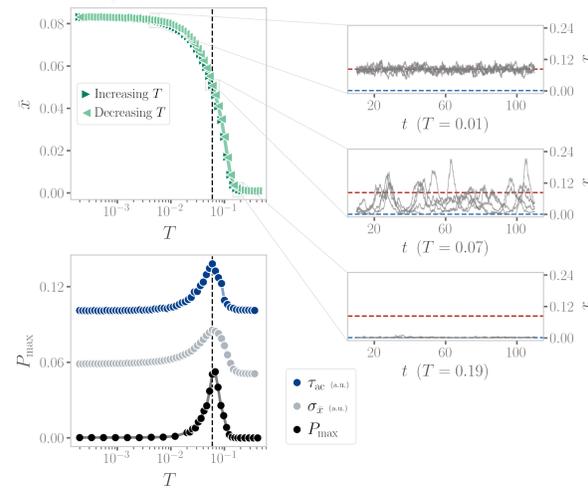
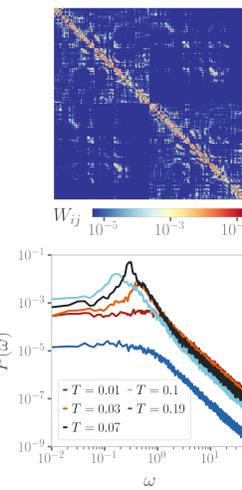


## ► CRITICALITY VS NETWORK STRUCTURE

● We embed the model in an **EMPIRICAL HUMAN CONNECTOME** and find that the complex network structure smooths the hysteresis cycles.

● At intermediate values of the threshold, the **AUTOCORRELATION TIME** and the **VARIANCE OF THE ACTIVITY** peaks, suggesting the presence of a **CRITICAL-LIKE TRANSITION**.

At the same threshold value, the **POWER-SPECTRUM** peaks due to the emergence of collective oscillations localized in subregions of the network.



● We find that both **NETWORK SPARSITY** and **WEIGHT HETEROGENEITY** are fundamental in smoothing the mean-field bistable region.

● However, sparsity and weights alone generate network-wide oscillations between the mean-field fixed point. **HIGHER-ORDER STRUCTURES** of the connectome are responsible for a smooth change of the dynamical fixed point and the emergence of local **COLLECTIVE OSCILLATIONS**.

In whole-brain models the underlying **NETWORK STRUCTURE** plays a crucial role and shapes the nature of dynamical transitions. In complex networks, a **CRITICAL-LIKE TRANSITION** appears and generates **COMPLEX EMERGENT BEHAVIORS**.

